3. (i) Find, in simplest form,

$$\int 2(3x+5)^7 \, dx$$

(2)

(ii) $$f(x) = \frac{4x^3 + x^2 - 7x + 14}{(x-1)(x+2)} \qquad x > 1$$

(a) Write $f(x)$ in the form

$$ax + b + \frac{c}{x-1}$$

where a, b and c are constants to be found.

(4)

(b) Hence, using algebraic integration, find

$$\int_3^9 f(x) \, dx$$

writing the answer in simplest form.

(4)

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Question 3 continued

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Question 3 continued

(Total for Question 3 is 10 marks)

4. The resting heart rate, h beats per minute, of a particular group of mammals, can be modelled by the equation

$$\log_{10} h = 2.4 - 0.25 \log_{10} m$$

where m kg is the mass of the mammal.

The mass of one of these mammals is 3 kg.

According to the model,

(a) find the resting heart rate of this mammal. Give your answer to 3 significant figures.

(2)

(b) Show that the equation of the model can be written in the form

$$h = \frac{p}{m^q}$$

giving each of the values of the constants p and q to 3 significant figures where appropriate.

(3)

(c) With reference to the model, interpret the value of the constant p.

(1)

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