5: **In this question you must show all stages of your working.**
Solutions relying entirely on calculator technology are not acceptable.

A curve C has equation

$$y = 5\cos 2x - 12\sin 2x \qquad -\pi < x < \pi$$

The point A with x coordinate $\frac{\pi}{3}$ lies on C.

(a) Use algebraic differentiation to find the gradient of the tangent to C at A.
Give the answer in simplest form.

(3)

(b) Express $5\cos 2x - 12\sin 2x$ in the form

$$R\cos(2x + \alpha)$$

where $R > 0$ and $0 < \alpha < \frac{\pi}{2}$

Find the exact value of R and find the value of α to 3 decimal places.

(3)

A point P lies on C.

Given that the gradient of the tangent to C at P is 6

(c) find the greatest possible value for the x coordinate of P.
Give the answer to 2 decimal places.

(4)

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Question 5 continued

Question 5 continued

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Question 5 continued

(Total for Question 5 is 10 marks)

6:

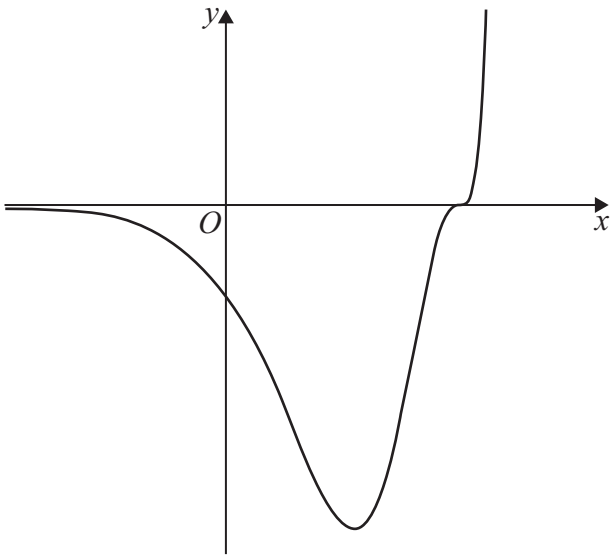

Figure 2

Figure 2 shows a sketch of the curve with equation $y = \mathrm{f}(x)$ where

$$\mathrm{f}(x) = (2x - 3)^3 \mathrm{e}^{4x-2}$$

(a) Show that

$$\mathrm{f}'(x) = 2(Px + Q)(2x - 3)^n \mathrm{e}^{4x-2}$$

where P, Q and n are constants to be found.

(4)

(b) Hence find

(i) the x coordinates of the stationary points on the curve with equation $y = \mathrm{f}(x)$,

(ii) the range of the function g defined by

$$\mathrm{g}(x) = 8(2x - 3)^3 \mathrm{e}^{4x-2} \qquad x \leqslant \frac{3}{2}$$

(*Solutions relying entirely on calculator technology are not acceptable.*)

(4)

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