10. **In this question you must show all stages of your working.**
Solutions relying entirely on calculator technology are not acceptable.

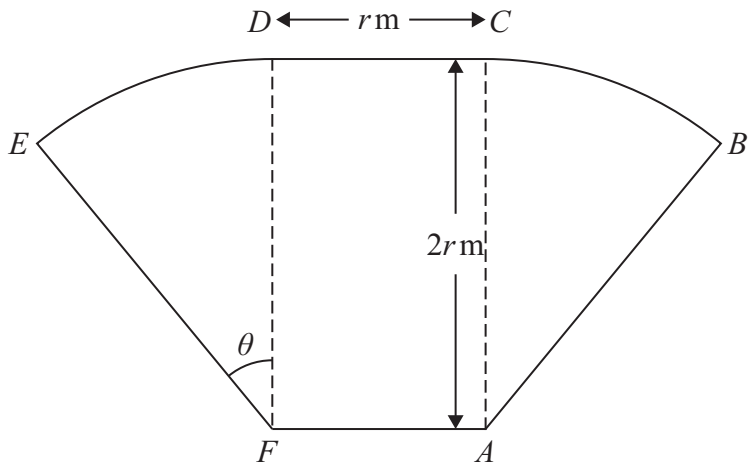


Figure 2

Figure 2 shows the plan view of the design for a stage at a trade fair.

The shape of the stage *ABCDEFA*, consists of a rectangle *ACDF* joined to two congruent sectors of circles. *ABC* is a sector of a circle centre *A* and *FDE* is a sector of a circle centre *F*.

Given that $AC = 2r$ metres, $CD = r$ metres, angle $DFE = \theta$ radians and the area of the stage is $30\,\text{m}^2$,

(a) show that the perimeter, *P* metres, of the stage, is given by

$$P = 4r + \frac{30}{r}$$

(4)

(b) Use calculus to find the minimum value for *P*, giving your answer in the form $a\sqrt{b}$, where *a* and *b* are integers to be found.

(4)

(c) Justify that the value of *P* found in part (b) is the minimum.

(2)

(Total for Question 10 is 10 marks)

TOTAL FOR PAPER IS 75 MARKS